

Proofs of Theorems and Glossary of Terms

Glossary of terms associated with theorems

<i>Axiom:</i>	An axiom is a statement which is assumed to be true and is used as a basis for developing a system. <i>Example: Axiom 1 - There is exactly one line through any two given points.</i>
<i>Converse:</i>	The converse of a theorem is formed by taking the conclusion as the starting point and having the starting point as the conclusion. <i>Example: The converse of Theorem 2 states 'If two angles are equal, then the triangle is isosceles'.</i>
<i>Corollary:</i>	A corollary follows after a theorem and is a proposition which must be true because of that theorem.
<i>Implies:</i>	Implies indicates a logical relationship between two statements, such that if the first is true then the second must be true.
<i>Proof:</i>	A proof is a sequence of statements (made up of axioms, assumption and arguments) leading to the establishment of the truth of one final statement.
<i>Theorem:</i>	A theorem is a statement which has been proved to be true.

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Just Click on the Proof Required

Theorem 4 Three angles in any triangle add up to 180° .

Theorem 6 Each exterior angle of a triangle is equal to the sum of the two interior opposite angles

Theorem 9 In a parallelogram opposite sides are equal and opposite angle are equal

Theorem 14 Theorem of Pythagoras : In a right angle triangle, the square of the hypotenuse is the sum of the squares of the other two sides

Theorem 19 The angle at the centre of the circle standing on a given arc is twice the angle at any point of the circle standing on the same arc.

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Theorem 4:

Three angles in any triangle add up to 180°C.

Use mouse clicks to see proof

Given: Triangle

To Prove: $\angle 1 + \angle 2 + \angle 3 = 180^\circ$

Construction: Draw line through $\angle 3$ parallel to the base

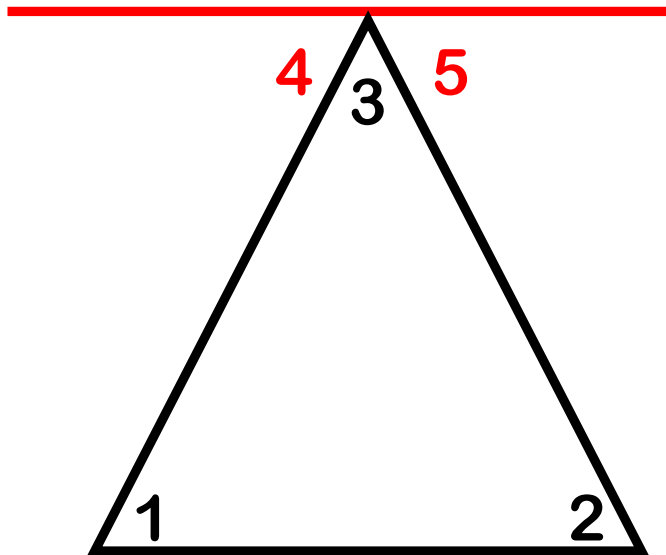
Proof: $\angle 3 + \angle 4 + \angle 5 = 180^\circ$ **Straight line**

$\angle 1 = \angle 4$ and $\angle 2 = \angle 5$ **Alternate angles**

$\Rightarrow \angle 3 + \angle 1 + \angle 2 = 180^\circ$

$\angle 1 + \angle 2 + \angle 3 = 180^\circ$

Q.E.D.



Constructions

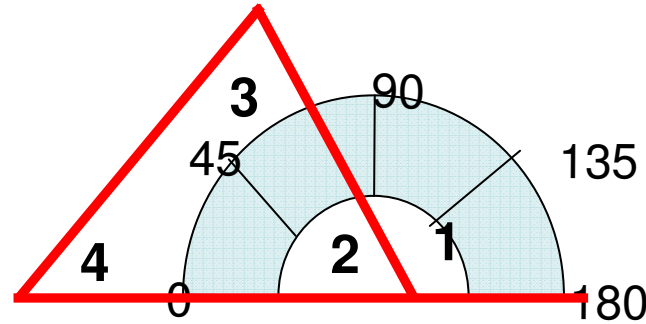
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Theorem 6:

Each exterior angle of a triangle is equal to the sum of the two interior opposite angles

Use mouse clicks to see proof



To Prove: $\angle 1 = \angle 3 + \angle 4$

Proof: $\angle 1 + \angle 2 = 180^\circ$ **Straight line**

$\angle 2 + \angle 3 + \angle 4 = 180^\circ$ **Theorem 2.**

$$\Rightarrow \cancel{\angle 1 + \angle 2} = \cancel{\angle 2} + \angle 3 + \angle 4$$

$$\Rightarrow \angle 1 = \angle 3 + \angle 4$$

Q.E.D.

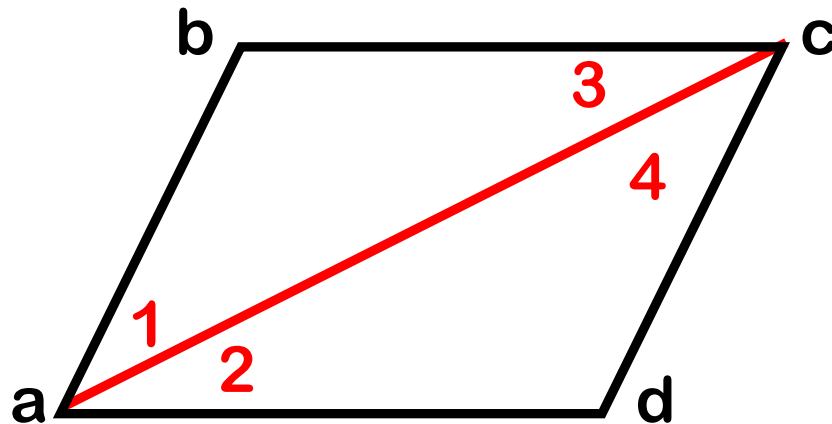
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Theorem 9: In a parallelogram opposite sides are equal and opposite angle are equal

Use mouse clicks to see proof



Given: Parallelogram abcd

To Prove: $|ab| = |cd|$ and $|ad| = |bc|$

and $\angle abc = \angle adc$

Construction: Draw the diagonal $|ac|$

Proof: In the triangle abc and the triangle adc

$\angle 1 = \angle 4$ Alternate angles

$\angle 2 = \angle 3$ Alternate angles

$|ac| = |ac|$ Common

\Rightarrow The triangle abc is congruent to the triangle adc **ASA = ASA.**

\Rightarrow $|ab| = |cd|$ and $|ad| = |bc|$

and $\angle abc = \angle adc$

Q.E.D

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Theorem 14: Theorem of Pythagoras : In a right angle triangle, the square of the hypotenuse is the sum of the squares of the other two sides

Use mouse clicks to see proof

Given: Triangle abc

To Prove: $a^2 + b^2 = c^2$

Construction: Three right angled triangles as shown

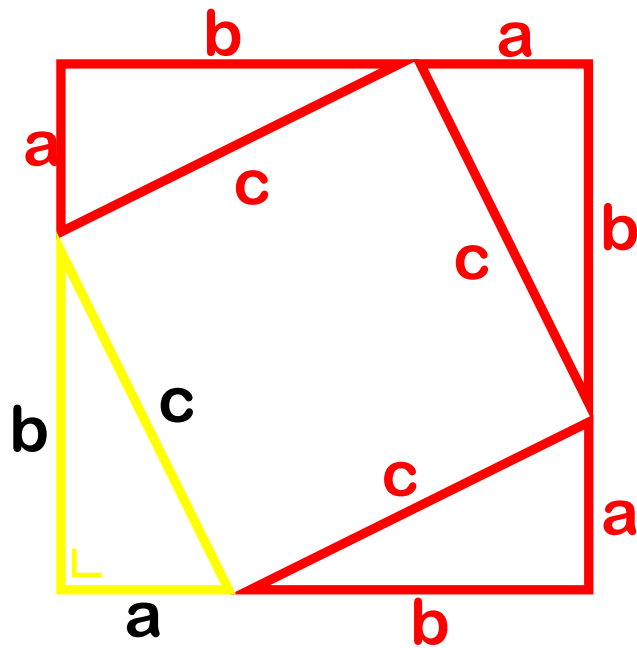
Proof: ** Area of large sq. = area of small sq. + 4(area Δ)

$$(a + b)^2 = c^2 + 4(\frac{1}{2}ab)$$

$$a^2 + 2ab + b^2 = c^2 + 2ab$$

$$a^2 + b^2 = c^2$$

Q.E.D.



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Theorem 19: The angle at the centre of the circle standing on a given arc is twice the angle at any point of the circle standing on the same arc.

Use mouse clicks to see proof

To Prove: $|\angle boc| = 2|\angle bac|$

Construction: Join a to o and extend to r

Proof: In the triangle aob

$|oa| = |ob|$ Radii

$\Rightarrow |\angle 2| = |\angle 3|$ Theorem 4

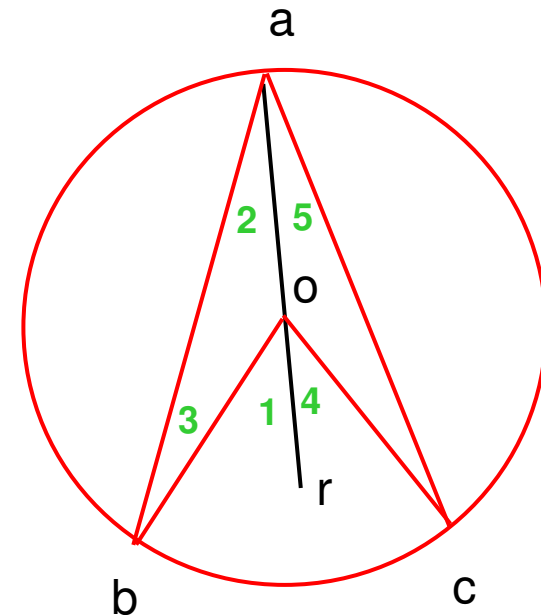
$|\angle 1| = |\angle 2| + |\angle 3|$ Theorem 3

$\Rightarrow |\angle 1| = |\angle 2| + |\angle 2|$

$\Rightarrow |\angle 1| = 2|\angle 2|$

Similarly $|\angle 4| = 2|\angle 5|$

$\Rightarrow |\angle boc| = 2|\angle bac|$ Q.E.D



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